

Fluid Mechanics(1)
Course No. 0904361
First Exam
Date: 25/3/2014

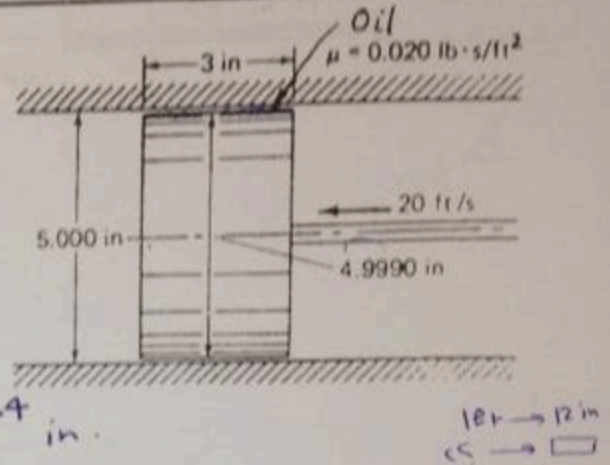
OPEN BOOK

Seat No.
Student Name: *علي بدران*
Student No. 0120361
Instructor: Prof. Ali Badran
Time: 60 Minutes

Prob. 1 (5 Points)

A piston is moving through a cylinder at a speed of 20 ft/s as shown. The film of oil separating the piston from the cylinder has a viscosity of $0.02 \text{ lb}\cdot\text{s}/\text{ft}^2$. What is the force required to maintain this motion?

Hint: Assume a linear velocity profile for the oil layer.



$$\mu = 0.020 \text{ lb}\cdot\text{s}/\text{ft}^2$$

$$u = 20 \text{ ft/s}$$

$$y = \frac{5.000 - 4.9990}{2} \Rightarrow y = 5 \times 10^{-4} \text{ in.}$$

$$y = 0.4167 \times 10^{-4} \text{ ft}$$

$$\tau = \mu \frac{du}{dy} \rightarrow \text{with linear velocity profile}$$

$$\frac{dy}{dy} = \frac{du}{du}$$

$$\tau = \frac{0.020 \times 20}{10^{-4} \times 0.4167} = (\tau = 0.96 \text{ lb}_f/\text{ft}^2)$$

$$\tau = \frac{F}{A} \Rightarrow A = 5 \times 3 = 15 \text{ in}^2$$

$$A = \frac{15}{(12)^2} = 0.1042 \text{ ft}^2$$

$$0.96 \times 10^4 \times 0.1042 = F$$

$$F = 0.1 \times 10^4 \text{ lb}_f$$

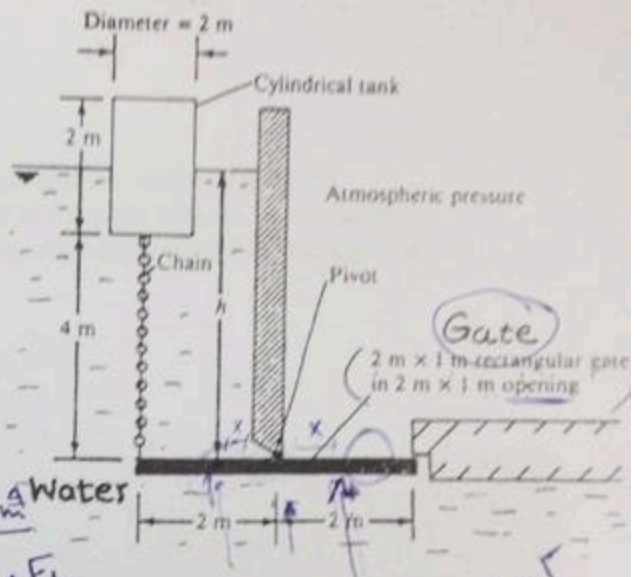
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Mech Family

Prob. 2 (7 Points)

The gate and mechanism shown are designed so that the gate will open when the level h reaches a certain value. Neglecting the weights of the gate, chain, and cylindrical tank, calculate the value of h at which the gate will start to open.



$$A_{\text{gate}} = 2 \times 1 = 2 \text{ m}^2$$

$$\bar{x} = h - 0.5 \text{ m}, \bar{x} = 1 \text{ m}$$

$$\bar{I}_{\text{gate}} = \frac{1}{12} b h^3 = \frac{1}{12} (4) (1)^3 = 0.33 \text{ m}^4$$

taking the cylinder:
weight is Neglegebile
so

$$\sum F_{\text{cylinder}} = 0$$

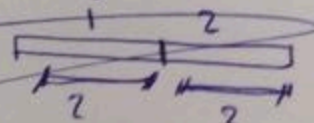
$$T = F_b \Rightarrow T = \gamma_{\text{fluid}} * V_{\text{object}}$$

$$T = 9810 * (h - 4) * \frac{\pi}{4} D^2$$

$$= 9810 * (h - 4) * 3.14$$

$$\textcircled{1} \quad T = 30819.0239 (h - 4) \text{ N}$$

~~F_v on Gate~~ $\Rightarrow$ we cut The gat to Two peaces



on Peace 1 $\Rightarrow F_{v1} = \gamma_{\text{fluid}} * V_{\text{gate1}} = 9810 * 0.141$

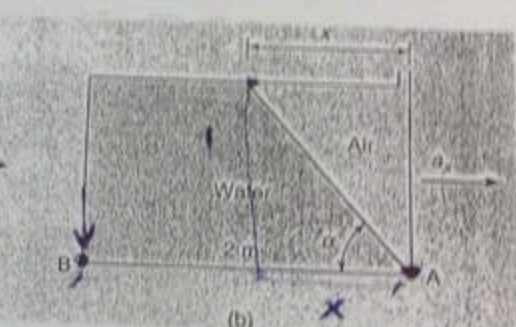
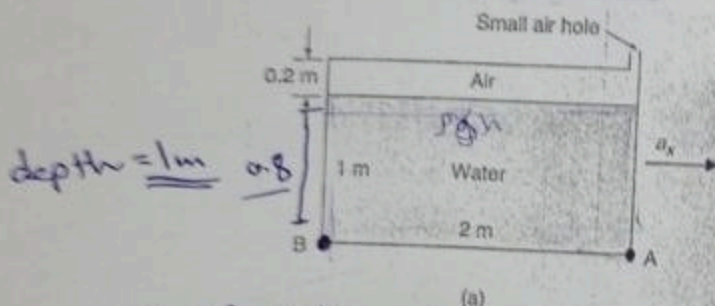


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Prob. 3 (8 Points)

The tank shown in the Figure (a) is rectangular in shape and the width of the tank (perpendicular to the paper) is 1 m. The tank is moved to the right with an acceleration a_x such that the free surface of the water makes an angle α with the bottom and touches it at point A, as shown in Figure (b). Calculate:

- The acceleration a_x .
- The gage pressure at point B.
- The total force acting on the bottom of the tank.



$$-\frac{\partial}{\partial x}(P + \gamma z) = \rho a_x$$

$$\int_B^A \partial(P + \gamma z) = \int_B^A \partial \rho a_x$$

$$\Rightarrow P_A + \gamma z_A - P_B - \gamma z_B = -\rho a_x (x_A - x_B)$$

$$P_A + 0 - P_B - 0 = -\rho a_x (2)$$

P_A is Atm pressure. we need gage pressure

$$P_B = \rho a_x \cdot 2000$$

$$\rho = \frac{\gamma}{g}$$