

11/12/2014

# Second Exam, 2014/2015 Engineering Measurements (0904422) (Key Solution)

Q1) - For accuracy  $\rightarrow$  check note / textbook.

- Flow Prover / catch and Weigh.

- For Selection  $\rightarrow$  check note / textbook.

- Vol<sup>m</sup> flow rate  $Q = \frac{1}{4} C_d \pi d_2^2 \sqrt{2g \frac{\Delta P_{1-2}}{\gamma_f}}$

Solving we get

$$d_2 = 60 \text{ mm}$$

- Pressure drop  $\Delta P_{1-2} = \gamma_f h_m \left[ \frac{S_{Gm}}{S_{Gf}} - 1 \right]$

$$\Rightarrow h_m = 2.87 \text{ m}$$

- To find pump  $\eta$  we need to find

Pressure loss  $\Delta P_{loss} = 75\% \Delta P_{1-2} = 266.7 \text{ kPa}$

Cost = time \* Power \* rate

$$\Rightarrow \text{Power} = 23.82 \text{ kW}$$

$$= \frac{Q_{act} * \Delta P_{loss}}{\eta_p}$$

$$\Rightarrow \eta_p = 89.5\%$$

- For Uncertainty  $Q = M \frac{1}{4} C_d A_2 \sqrt{\frac{2}{\gamma_f} \Delta P_{1-2}}$

$\Phi$  is Constant

$$= \Phi M C_d A_2 \Delta P^{\frac{1}{2}}$$

$$\therefore \frac{\Delta Q}{Q} = \pm \sqrt{\left( \frac{\Delta M}{M} \right)^2 + \left( \frac{\Delta C_d}{C_d} \right)^2 + \left( \frac{\Delta A_2}{A_2} \right)^2 + \left( \frac{1}{2} \frac{\Delta \Delta P}{\Delta P} \right)^2}$$

$$\therefore \frac{\Delta \Delta P_{1-2}}{\Delta P_{1-2}} = \pm 0.051 \Rightarrow \Delta \Delta P = \pm 18.135 \text{ kPa}$$



Q2) - For factors check note / textbook.

$$\begin{aligned} \text{(Static Press)} \quad P_{\text{static}} &= P_{\text{atm}} + \gamma_m h_{m1} & P_{\text{atm}} &= 760 \text{ mm Hg} \\ &= \frac{760}{1000} \times 13600 \times 9.81 + \frac{9810 \times 10}{1000} \end{aligned}$$

$$= 101.886 \text{ kPa}$$

$$P_{\text{stagnation}} = P_{\text{atm}} + \gamma_m h_{m2}$$

$$P_s = 102.181 \text{ kPa}$$

$$\text{Flow Velocity } (V_f) = C \sqrt{\frac{2}{\rho_f} \Delta P} = 22.3 \text{ m/s}$$

Q3) - main criteria  $\delta_m < \frac{1}{2} t$  so that the deflection is linear and max<sup>m</sup> at center.

$$\text{- Thickness } t = \sqrt{\frac{3 D^2 P}{16 \sigma_m}} = 1.94134 \times 10^{-3} \text{ m}$$

$$\text{- Deflection } \delta_m = \frac{3(1-\nu^2) D^4 P}{256 E t^3} = 1.1924 \times 10^{-5} \text{ m}$$

$> \frac{1}{2} t$  hence the thickness must be changed. At  $t = 2.1 \text{ mm} \Rightarrow \delta_m = 0.948 \text{ mm}$

$$= \frac{C_i}{C_f} = \frac{(E_f / D_f) \cdot A_i / d_i}{(E_f / D_f) \cdot A_f / d_f} = \frac{d_i - \delta_m}{d_i}$$

$$\therefore C_f = 506.215 \text{ PF}$$



Q4) - For qualities check note / textbook.  
- Best mathematical law is the quadratic  
range -30 - 0

$$239.58 = 423.58 \left[ 1 + \alpha_1(-30-0) + \alpha_2(-30-0)^2 \right]$$

range 0 - 110

$$6484.3 = 423.58 \left[ 1 + \alpha_1(110-0) + \alpha_2(110-0)^2 \right]$$

Solving we get

$$\alpha_1 = 0.03925$$

$$\alpha_2 = 8.256 \times 10^{-4}$$

$$\therefore R_T = 423.58 \left[ 1 + 0.03925(T-0) + 8.256 \times 10^{-4}(T-0)^2 \right]$$

$$\text{- At } R_T = 3848.242 \Rightarrow \boxed{T = 78^\circ\text{C}}$$

-  $120^\circ\text{C}$  is out-of-range.

$$\text{Q5) - } V_{i \text{ max}} = \sqrt{P R_f} = \sqrt{3 \times 5200}$$

$$= 122.47 \text{ Volts.}$$

- Cermet, - Carbon film, - Hot moulded Carbon

Q6) - Wire, Foil, Semiconductor

$$\text{- } \Delta R_{Ni} = R_i \alpha G_f = +7.26 \times 10^3 \Omega$$

$$\therefore R_{\text{final}} = \boxed{120.00726 \Omega}$$

$$\Delta R_{\text{Nichrome}} = -12 \times 10^{-3} \Omega \Rightarrow R_{\text{final}} = \boxed{199.998 \Omega}$$



Q7) - For Comparison check note/textbook.

$$R_{T_2} = R_{T_1} e^{\beta \left( \frac{1}{T_2} - \frac{1}{T_1} \right)}$$

$$\text{or } 10/17 = 8632.371 e^{\beta \left( \frac{1}{413} - \frac{1}{283} \right)}$$

$$\therefore \beta = 3997.686 \text{ K}$$

$$\text{- At } T = 280^\circ \text{C} \Rightarrow R_T = 524.3 \Omega$$